EBBING - GAMMON

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The Gaseous State

General Chemistry ELEVENTH EDITION

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Low molecular weight

Most substances composed of small molecules are gases under normal conditions or else are easily vaporized liquids

> Gas Laws 8

Table 5.1 Properties of Selected Gases(Liquid \rightarrow gas)				
Name	Formula	Color 🗶	Odor K	Toxicity 🗙
Ammonia	NH ₃	Colorless	Penetrating	Toxic
Carbon dioxide	CO ₂	Colorless	Odorless	Nontoxic
Carbon monoxide	CO	Colorless	Odorless	Very toxic
Chlorine	Cl ₂	Pale green	Irritating	Very toxic
Hydrogen	H ₂	Colorless	Odorless	Nontoxic
Hydrogen sulfide	H_2S	Colorless	Foul	Very toxic
Methane	CH ₄	Colorless	Odorless	Nontoxic
Nitrogen dioxide	NO ₂	Red-brown	Irritating	Very toxic



Pressure of a coin (9.3 mm in radius and 2.5 g)
Force = mass x g = (2.5 x10⁻³ kg) × (9.81 m/s²)
Area =
$$\pi$$
 x (radius)² = 3.14 x (9.3 × 10⁻³ m)²
For the 25g × (9.8 × 10 - g)
Pressure = $\frac{\text{force}}{\text{area}} = \frac{(2.5 \times 10^{-2}) \text{kg} \cdot \text{m/s}^2}{2.7 \times 10^{-4} \text{m}^2} = 93 \text{ kg/(m \cdot s^2)} = 93 \text{ Pa}$

 The general relationship between the pressure *P* and the height *h* of a liquid column in a barometer or manometer is:







Boyle's experiment:

The volume of the gas at normal atmospheric pressure (760 mmHg) is 100 mL. When the pressure is doubled by adding 760 mm of mercury, the volume is halved (to 50 mL).

Tripling the pressure decreases the volume to one-third of the original (to 33 mL). 6



(Q) A volume of air occupying 12.0 dm³ at 98.9 kPa is compressed to a pressure of 119.0 kPa. The temperature remains constant. What is the new volume?

Is the new volume?

$$P_i V_i = P_f V_f$$

$$Reminder!$$

$$V_f = V_i \times \frac{P_i}{P_f} = 12.0 \text{ dm}^3 \times \frac{98.9 \text{ kPa}}{119.0 \text{ kPa}} = 9.97 \text{ dm}^3 \text{ fl}$$

Exan

For cise 5.1 A gas in a container had a measured pressure of
57 kPa. Calculate the pressure in units of atm and mmHg.
* 57 K Pa
$$\therefore$$
 1 atm \longrightarrow mmHg \Rightarrow $1 \text{ atm} = 1.0325 \times 10^{5} \text{ p}$
57 K pa \times 1 atm 101 K pa $= [5564 \text{ atm}]$ \times $1 \text{ atm} = 1.0325 \times 10^{5} \text{ p}$
 $57 \text{ K pa} \times$ 1 atm 101 K pa $= [5564 \text{ atm}]$ \times $160 \text{ mmHg} = 1 \text{ atm}$
 $\cdot 564 \text{ atm} \times$ $\frac{760 \text{ nmHg}}{1 \text{ atm}}$ $=$ $428,64 \text{ mmHg} \longrightarrow$ $\left[4.3 \times 10^{3} \text{ mmHg}\right]$
For cise 5.2 A volume of carbon dioxide gas, CO₂ equal to 20.0 L was collected at 23°C and 1.00 atm pressure.
What would be the volume of carbon dioxide collected at 23°C and 0.830 atm?
 $(\text{Pi} \times \text{Ni} = \text{Pf} \times \text{VF})$
 $20.0 L \times 1.0 \text{ atm} = \text{Vf} \times .830 \text{ atm}$ $23C^{\circ} - CO2$
At given Amount of $\frac{100 \text{ mm}}{7 \text{ mm}}$ for $\frac{100 \text{ mm}}{7 \text{ mm}}$ and $\frac{100 \text{ mm}}{7 \text{ mm}}$ and $\frac{100 \text{ mm}}{7 \text{ mm}}$ for $\frac{1000 \text{ mm}}{7 \text{ mm}}}$ for $\frac{1000 \text{ mm}}{7 \text{ mm}}$ for $\frac{1000 \text{ mm}}{7 \text{ mm}}$ for $\frac{1000 \text{ mm}}{7 \text{ mm}}$ for $\frac{1000 \text{ mm}}{7 \text{ mm}}}$ for $\frac{1000 \text{ mm}}{7 \text{ mm}}$ for $\frac{1000 \text{ mm}}{7 \text{ mm}}}$ for $\frac{1000 \text{ mm}}{7 \text{ mm}}$ for $\frac{1000 \text{ mm}}{7 \text{ mm}}}$ for $\frac{1000 \text{ mm}}{7 \text{ mm}}$ for $\frac{1000 \text{ mm}}{7 \text{ mm}}}$ for $\frac{1000 \text{ mm}}{7 \text{ mm}}}$ for $\frac{1000 \text{$



Exercise 5.3 If you expect a chemical reaction to produce 4.38 dm³ of oxygen, O_2 , at 19°C and 101 kPa, what will be the volume at 25°C and 101 kPa?



First, convert the temperatures to the Kelvin. T = (19 + 273) = 292 K

$$T_f = (25 + 273) = 298 \text{ K}$$

Apply Charles's law

$$V_f = V_i \times \frac{T_f}{T_i} = 4.38 \text{ dm}^3 \times \frac{298 \text{ K}}{292 \text{ K}} = 4.47 \text{ dm}^3$$

Example 5.3

Earlier we found that the total volume of oxygen that can be obtained from a particular tank at 1.00 atm and 21°C is 785 L (including the volume remaining in the tank). What would be this volume of oxygen if the temperature had been 28°C?

$$T_{i} = 21C' + 273 = \frac{294K}{301K}$$

$$\frac{\sqrt{1}}{1} = \frac{\sqrt{1}}{1} \xrightarrow{785L} = \frac{\sqrt{2}}{301 \text{ k}}$$

$$\longrightarrow 804 \text{ L}$$
9

Combined Gas Law: Relating Volume, Temperature, and Pressure

✓ Boyle's law ($V \alpha 1/P$) and Charles's law ($V \alpha T$) can be combined to:

V α *T*/P

 $V = \text{constant} \times \frac{I}{P}$ or $\frac{PV}{T} = \text{constant}$ (for a given amount of gas) It must be in Kelvin $\frac{P_f V_f}{T_f} = \frac{P_i V_i}{T_i}$ Reminder (Example 5.4 Given amount of gas (\mathcal{Q}) A 39.8 mg sample of caffeine gives 10.1 cm³ of N₂ gas at 23°C and 746 mmHg. What is the volume of N₂ at 0°C and 760 mmHg? $T_i = (23 + 273) \text{ K} = 296 \text{ K}$ $T_f = (0 + 273) \text{ K} = 273 \text{ K}$ $V_f = V_i \times \frac{P_i}{P_f} \times \frac{T_f}{T_i} = 10.1 \text{ cm}^3 \times \frac{746 \text{ mmHg}}{760 \text{ mmHg}} \times \frac{273 \text{ K}}{296 \text{ K}} = 9.14 \text{ cm}^3$ 10

(2) What will be the final pressure of a sample of nitrogen gas with a volume of 950. m³ at 745 torr and 25.0 °C if it is heated to 60.0 °C and given a final volume of 1150 m³?

A balloon contains 5.41 dm³ of helium, He, at 24°C and 101.5 kPa. Suppose the gas in the balloon is heated to 35°C. If the helium pressure is now 102.8 kPa, what is the volume of the gas?

$$T_i = (24 + 273) = 297 \text{ K}$$

 $T_f = (35 + 273) = 308 \text{ K}$

$$V_f = V_i \times \frac{P_i}{P_f} \times \frac{T_f}{T_i} = 5.41 \text{ dm}^3 \times \frac{101.5 \text{ kPa}}{102.8 \text{ kPa}} \times \frac{308 \text{ K}}{297 \text{ K}} = 5.539 = 5.54 \text{ dm}^3$$

1. V~T Charles 2. $\sqrt{\frac{1}{\rho}}$ Boyles $\sqrt{\frac{1}{\rho}}$ law $\sqrt{\frac{1}{\rho}}$ Constant $\times \frac{1}{\rho}$ V = C onstant T law \underline{V} = Constant $\rho \times V = Constant^{\rho}$ $\frac{V_1}{T_1} = \frac{V_2}{T_2} = \frac{V_3}{T_3} = Constant$ $\rho_{1} \overline{V}_{1} = \rho_{2} \overline{V}_{2} = \rho_{3} \overline{V}_{3} = Constant$ $\rho_{1} \overline{V}_{1} = \rho_{p} \overline{V}_{p}$ $\frac{\not(V_i)}{T_i} = \frac{\sqrt{p}}{T_i}$ $V = Constant T P_i V_i = P_e$ $PV = Constant^{P} T_{i}$ TA $\rho, \overline{V}, \rho_2 \overline{V}_2 \rho_3 \overline{V}_3$, VX T



= Constant n * (atm) Constant = R N n (mol) ¥ = 0.0821 atm. L/mol.k PV = nRTR Ldeal Law gas Explanation

> 5.3 The Ideal Gas Law
$$PV = nRT$$
 Removed Example 5.6
(Q) How many grams of oxygen are there in a 50.0-L gas cylinder
at 21°C when the oxygen pressure is 15.7 atm?
 $PV = \frac{m}{mm} RT \Rightarrow 15.7 \times 50.0 = \frac{m}{31.098} \times 2944 \times 0.0821$
Exercise 5.6
($m = 1040.64g = 1.04.10^3g$)
What is the pressure in a 50.0-L gas cylinder that contains 3.03 kg
of oxygen, O_2 , at 23°C?
 $PV = nRT = r P \times 50.0 = \frac{3.03 \times 10}{31.998} \times 0.0821 \times 296 = \frac{1}{31.998}$
($p = 46.02$ dtm)
(a) Calculate the volume (in L) occupied by 7.40 g of NH₃ at STP
 $PV = nRT$
 $PV = nRT$
 $PV = nRT$
 $= 9.74 L$

Example 5.5 Deriving Empirical Gas Laws from the Ideal Gas Law

Gaining Mastery Toolbox

Critical Concept 5.5

The ideal gas law can be used to derive relationships between *n*, *P*, *T*, and *V*. Interpreting the equation PV = nRT can lead you to the relationships between each of the variables. For example, for a sample of gas the pressure (*P*) is directly proportional to the number of moles (*n*) of gas and the temperature (*T*) of the gas.

Solution Essentials:

- Ideal gas law (PV = nRT)
- Units of pressure (Table 5.2)
- Kelvin temperature

Prove the following statement: the pressure of a given amount of gas at a fixed volume is proportional to the absolute temperature. This is sometimes called *Amontons's law.* In 1702, Guillaume Amontons constructed a thermometer based on measurement of the pressure of a fixed volume of air. The principle he employed is now used in special gas thermometers to establish the Kelvin scale.

Problem Strategy Because we need a relationship between pressure and temperature, the ideal gas law is a logical starting place.

Solution From the ideal gas law,

PV = nRT

Solving for P, you get

 $P = \left(\frac{nR}{V}\right)T$

Note that everything in parentheses in this equation is constant. Therefore, you can write

 $P = \text{constant} \times T$

Or, expressing this as a proportion,

 $P \propto T$

Boyle's law and Charles's law follow from the ideal gas law by a similar derivation. *(continued)*

Exercise 5.5 Show that the moles of gas are proportional to the pressure for constant volume and temperature.

$$PV = nRT^* \rightarrow P = n\underline{R}_{\mathcal{A}}$$
 Constant
 $P = n \times Constant \rightarrow ((P \propto n))$

Molarity $PV = nR^{-1}$ * n RT MRT 8 ¥ _ x RT M mm PMm = dRT x RT TP M Densitu > P Mm = dRT

Gas Density; Molecular-Weight Determination



(Q) What is the density of oxygen, O₂, in grams per liter at 25°C and 0.850 atm?

 $d = PM_m/RT = (0.85 \times 32)/(0.082 \times 298) = 1.11 g/L$

Exercise 5.8 A sample of a gaseous substance at 25°C and 0.862 atm. has a density of 2.26 g/L. What is the molecular weight of the substance?

 $M_{m} = dRT/P = (2.26 \times 0.082 \times 298) / 0.862 = 64.1 \text{ g/mol}$ $1 \text{ mL} = 1 \text{ cm}^{3}$









5.4 Stoichiometry Problems Involving Gas Volumes

 $6NaN_3(s) + Fe_2O_3(s) \rightarrow 3Na_2O(s) + 2Fe(s) + 9N_2(g)$

Calculate the volume of N_2 generated at 80°C and 823 mmHg by the decomposition of 60.0 g of NaN₃

Exercise 5.9 How many liters of chlorine gas, Cl₂, can be obtained at 40°C and 787 mmHg from 9.41 g of hydrogen chloride, HCl, according to the following equation?

 $2KMnO_{4}(s) + 16HCl(aq) \rightarrow 8H_{2}O(l) + 2KCl(aq) + 2MnCl_{2}(aq) + 5Cl_{2}(g)$ $9.41gHCL \times \frac{1 \mod HCl}{36.46g} \times \frac{5'CL}{16HCl} \underbrace{00821 \times 313'}_{1.035} (20.L)$ 15

Example 5.9: 123 + Fe 2 03 (s) - $3Na_2O_{(s)} + 2Fe_{(s)} + 9N_2 (s)$





Explanation PT = PA + PB + Pc + ···· * Constant T. V
 Total
 $\frac{n_{T}RT}{V} = \frac{n_{A}RT}{V} + \frac{n_{B}RT}{V} + \frac{n_{C}RT}{V}$ $\frac{N_T RT}{J} = \frac{RT}{J} \left(na + nB + nc + \dots \right)$ $nT = (na + NB + Nc + \dots)$ $\frac{n_a}{a} = \frac{P_A}{A} = X_A \longrightarrow \text{mole Fraction}$ N T PT

Dalton's law of partial pressures: $P_{T} = P_{A} + P_{B} + P_{C} + \cdots$

✓ The individual (partial pressures) follow the ideal gas law. For $\sqrt{1} = n_A RT$ component A,

Mole fraction of
$$A = \frac{n_A}{n} = \frac{P_A}{P}$$



(Q) A 1.00-L sample of dry air at 25°C and 786 mmHg contains 0.925 g N₂, plus other gases including oxygen, argon, and carbon dioxide. a. What is the partial pressure (in mmHg) of (N_2) in the air sample? b. What is the mole fraction and mole percent of N_2 in the $0.925 \text{ g } N_2 \times \frac{1 \text{ mol } N_2}{28.0 \text{ g } N_2} = 0.0330 \text{ mol } N_2$ Hixture mixture? $\frac{n_{N_2}RT}{V_{C}} = \frac{0.0330 \text{ mol} \times 0.0821 \text{ V} \cdot \text{atm}/(\text{K} \cdot \text{mol}) \times 298 \text{ K}}{\text{Mixture / Sample } 1.00 \text{ V}} = 0.807 \text{ atm} (= 613 \text{ mmHg})$ $\frac{P_{\rm N_2}}{P} = \frac{613 \,\rm mmHg}{786 \,\rm mmHg} =$ / واحر ٢٠٠) + مابير استقام Air contains 78.0 mole Mole fraction of N₂ 0.780 percent of N₂.

mm H9

(Q) Each of the color spheres represents a different gas molecule. Calculate the partial pressures of the gases if the total pressure is 2.6 atm.

Mole fraction of
$$A = \frac{n_A}{n} = \frac{P_A}{P}$$

* $X_r = \frac{4}{12} = .333 \text{ mol}$
* $X_b = \frac{2}{12} = .166 \text{ mol}$
* $X_g = \frac{6}{12} = .5 \text{ mol}$
* $X_g = \frac{6}{1$

(Q) A mixture consists of 122 moles of N₂, 137 moles of C₃H₈, and 212 moles of CO₂ at 200 K in a 75.0 L container. What is the total pressure of the gas and the partial pressure of CO₂? A. 46.4 atm, 20.9 atm $\mathbf{N_T} = \frac{\mathbf{K} \cdot \mathbf{R}}{(471 \text{ moles})(0.0821 \text{ L atm} \text{ mol}^{-1} \text{ K}^{-1})(200 \text{ K})}$ B. 103 atm, 26.7 atm $\mathbf{N} \cdot \mathbf{P}_{\text{total}} = \frac{(471 \text{ moles})(0.0821 \text{ L atm} \text{ mol}^{-1} \text{ K}^{-1})(200 \text{ K})}{\mathbf{V} \cdot \mathbf{V}}$ $P_{total} = 103 \text{ atm}$ C. 103 atm, 46.4 atm **2** mole fraction CO₂: $\frac{212 \text{ moles CO}_2}{122 + 137 + 212 \text{ total}} = 0.450$ D. 103 atm, 29.9 atm E. 46.4 atm, 46.4 atm $P_{CO_2} = (\chi_{CO_2})(P_{total}) = (0.450)(103 \text{ atm})$ Partial presure Co2 $P_{CO_{2}} = 46.4 \text{ atm}$ $P = \frac{nRT}{-T} = 46.4$ Mole fraction of $A = \frac{n_A}{n} = \frac{P_A}{P}$

(\mathcal{Q}) A mixture of 250 mL of methane, CH₄, at 35° C) and 0.55 atm and 750 mL of propane, C_3H_8 , a (35° C) and 1.5 atm was introduced into a 10.0 L container. What is the mole fraction of methane in the mixture? $P_1V_1 = P_2V_2$ $\frac{0.55 \text{ atm } \times 0.250 \text{ L}}{10.0 \text{ L}} = 0.0138 \text{ atm}$ A. 0.50 *Р*сн₄ = Mole fraction of $A = \frac{n_A}{d} = \frac{n_A}{d}$ P_A **B.** 0.11 $\frac{1.5 \text{ atm } \times 0.750 \text{ L}}{1.5 \text{ atm }} = 0.112 \text{ atm}$ $P_{C_3H_8}$ C. 0.89 Partial pressure J -10.0 L PCH4 لل gas م يجد أت D. 0.25 0.0138 atm = 0.110 χ_{CH_4} – 0.0138 atm + 0.112 atm E. 0.33 alsil (Volume y) Pp Tote V Total Boyle'S law Tempretw $\mathcal{L}_{\text{volume C3Hr}} = 5.4 \times 10^{3} (n)$ Jolume CH4 Compined law I purie n = pV $\frac{P_1 \sqrt{1}}{T_1} = \frac{P_2 \sqrt{2}}{T_2}$ RT = 0.044 mol n elly 20n Total

See Problems 5.81, 5.82, **Exercise 5.10** A 10.0-L flask contains $1.031 \text{ g } O_2$ and 0.572 g $\overline{\text{CO}}_2$ at 18°C. What are the partial pressures of oxygen and 5.83, and 5.84. carbon dioxide? What is the total pressure? What is the CHEM mole fraction of oxygen in the mixture? Volume = 10.0L T = 291 K° +1 $O_2 = 1.031g - 0.572g = Co2 - T = 8C^{2}$ 1) portial presure O2 = pO2 ____ nRT $N = \frac{1.031}{32. \text{ glmol}} = 0.0322 \text{ mol} \quad \sqrt[n]{\sqrt{2}} \quad N = \frac{m}{N}$ $\frac{1.031}{32. \text{ glmol}} = 0.0322 \text{ mol} \quad \sqrt[n]{\sqrt{2}} \quad N = \frac{m}{N}$ mm - 0.0769 atm 1- 10.0/ 2) portial presure Co2 = PCo2 => nRT M = 0.5729 = .013 mol - n62 Vmm

3) Total presure = PC02 + PO2 0.0769 + 0.031 =,1079 atm 4.) The mole Praction O 2 ?? X 02 = 101PO2 hт .1079 0.0451



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