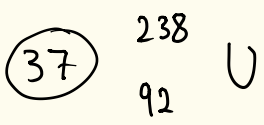


② $r = 1.2 \times 10^{-15} \text{ A}^{\frac{1}{3}}$
 $= 1.2 \times 10^{-15} \times 4^{\frac{1}{3}} = 1.905 \times 10^{-15} \text{ m}$
 $= 1.905 \text{ fermi}$



a) decay constant $\Rightarrow \lambda$

$\lambda = \frac{\ln 2}{t_{\frac{1}{2}}} = \frac{\ln 2}{(4.5 \times 10^9) \text{ yr}} = 1.54 \times 10^{-10} \text{ yr}^{-1}$

b) $\lambda = \frac{\ln 2}{t_{\frac{1}{2}}} \Rightarrow t_{\frac{1}{2}} = \frac{\ln 2}{\lambda} = \frac{\ln 2}{(3.2 \times 10^{-5}) \text{ s}^{-1}} = 21,660.94 \text{ s}$



Iodine - 131

(1) Atomic Number Z	(2) Element	(3) Symbol	(4) Mass Number A	(5) Atomic Mass	(6) % Abundance (or Radioactive Decay Mode)	(7) Half-life (if radioactiv)
52	Tellurium	Te	130	129.906223	34.08%; $\beta^- \beta^-$	$> 3.0 \times 10^8$ yr
53	Iodine	I	127	126.904472	100%	
			131	130.906126	β^-, γ	8.0252 d
54	Xenon	Xe	132	131.904155	26.9086%	
			136	135.907214	8.8573%; $\beta^- \beta^-$	$> 2.4 \times 10^8$ yr
55	Cesium	Cs	133	132.905452	100%	
56	Barium	Ba	137	136.905827	11.232%	
			138	137.905247	71.698%	
57	Lanthanum	La	139	138.906356	99.9119%	
58	Cerium	Ce	140	139.905443	88.450%	
59	Praseodymium	Pr	141	140.907658	100%	
60	Neodymium	Nd	142	141.907729	27.152%	
61	Promethium	Pm	145	144.912756	EC, α	17.7 yr
62	Samarium	Sm	152	151.919740	26.75%	
63	Europium	Eu	153	152.921238	52.19%	
64	Gadolinium	Gd	158	157.924112	24.84%	
65	Terbium	Tb	159	158.925355	100%	
66	Dysprosium	Dy	164	163.929182	28.260%	
67	Holmium	Ho	165	164.930329	100%	
68	Erbium	Er	166	165.930300	33.503%	
69	Thulium	Tm	169	168.934218	100%	
70	Ytterbium	Yb	174	173.938866	31.026%	
71	Lutetium	Lu	175	174.940775	97.401%	
72	Hafnium	Hf	180	179.946557	35.08%	
73	Tantalum	Ta	181	180.947996	99.98799%	
74	Tungsten (wolfram)	W	184	183.950931	30.64%; α	$> 8.9 \times 10^8$ yr
75	Rhenium	Re	187	186.955750	62.60%; β^-	4.33 $\times 10^4$ yr
76	Osmium	Os	191	190.960926	β^-, γ	15.4 days
			192	191.961477	40.78%	
77	Iridium	Ir	191	190.960589	37.3%	
			193	192.962922	62.7%	
78	Platinum	Pt	195	194.964792	33.78%	
79	Gold	Au	197	196.966569	100%	
80	Mercury	Hg	199	198.968281	16.87%	
			202	201.970643	29.86%	
81	Thallium	Tl	205	204.974428	70.48%	
82	Lead	Pb	206	205.974466	24.1%	
			207	206.975897	22.1%	
			208	207.976652	52.4%	
			210	209.984189	β^-, γ, α	22.20 yr
			211	210.988737	β^-, γ	36.1 min
			212	211.991898	β^-, γ	10.64 h
			214	213.999806	β^-, γ	26.8 min
83	Bismuth	Bi	209	208.980399	100%	
			211	210.987270	α, γ, β^-	2.14 min
84	Polonium	Po	210	209.982874	$\alpha, \gamma, \text{EC}$	138.376 da
			214	213.995202	α, γ	164.3 μs
85	Astatine	At	218	218.008695	α, β^-	1.5 s

$$t_{\frac{1}{2}} = 8.0252 \text{ days}$$

$$m = 782 \mu\text{g} = 782 \times 10^{-6} \text{ g}$$

from m , we can find number of moles and then N_0

$$782 \times 10^{-6} \cancel{\text{g}} \times \frac{1 \cancel{\text{mol}}}{131 \cancel{\text{g}}} \times \frac{6.02 \times 10^{23} \text{ nuclei}}{1 \cancel{\text{mol}}}$$

Avogadro number

$$N_0 = 3.59 \times 10^{18} \text{ nuclei}$$

$$\lambda = \frac{\ln 2}{t_{\frac{1}{2}}} = \frac{\ln 2}{8.0252 \text{ days}} = 0.08637 \text{ days}^{-1}$$

from table

Standard units of λ is s^{-1} , so we need to convert $\text{day}^{-1} \longrightarrow \text{s}^{-1}$

$$\frac{0.08637}{1 \cancel{\text{day}}} \times \frac{1 \cancel{\text{day}}}{24 \cancel{\text{h}}} \times \frac{1 \cancel{\text{h}}}{60 \cancel{\text{min}}} \times \frac{1 \cancel{\text{min}}}{60 \text{ s}}$$

$$\lambda (\text{s}^{-1}) = 9.9668 \times 10^{-7} \text{ s}^{-1}$$

$$A_0 = \lambda N$$

$$= 9.9668 \times 10^{-7} \text{ s}^{-1} \times 3.59 \times 10^{18} \text{ nuclei}$$

$$= \boxed{3.59 \times 10^{12} \frac{\text{decays}}{\text{s}}}$$

$$b) \quad A = A_0 e^{-\lambda t}$$

$$t = 1.5 \text{ h} \Rightarrow (1.5 \times 60 \times 60) \text{ s} = 5400 \text{ s}, \quad A = ?, \quad \lambda = 9.99668 \times 10^{-7}$$

$$A_0 = 3.59 \times 10^{12} \text{ (previous Q)}$$

$$A = (3.59 \times 10^{12}) e^{-(9.99668 \times 10^{-7})(1.5 \times 60 \times 60)}$$

$$= \boxed{3.573 \times 10^{12} \frac{\text{decays}}{\text{s}}}$$

c) 3 months:

$$3 \text{ months} \times \frac{30 \text{ days}}{1 \text{ month}} \times \frac{24 \text{ h}}{1 \text{ day}} \times \frac{60 \text{ min}}{1 \text{ h}} \times \frac{60 \text{ s}}{1 \text{ min}}$$

$$t \text{ (s)} = 7,776,000$$

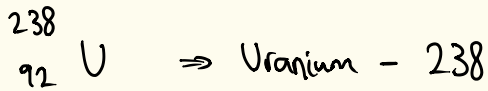
$$A = A_0 e^{-\lambda t}$$

$$A = (3.59 \times 10^{12}) e^{-(9.99668 \times 10^{-7})(7,776,000)}$$

$$A = 1,511,592,067 \frac{\text{decays}}{\text{s}}$$

$$= \boxed{1.51 \times 10^9 \frac{\text{decays}}{\text{s}}}$$

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$$\lambda = \frac{\ln 2}{t_{\frac{1}{2}}} = \frac{\ln 2}{4.468 \times 10^9 \text{ yr}}$$

$$\lambda = 1.55135 \times 10^{-10} \text{ yr}^{-1}$$

$$\lambda = \frac{1.55135 \times 10^{-10}}{1 \text{ yr}} \times \frac{1 \text{ yr}}{365 \text{ days}} \times \frac{1 \text{ day}}{24 \times 60 \times 60 \text{ s}}$$
$$= 4.919 \times 10^{-18} \text{ s}^{-1}$$

$$A = \lambda N$$

$$\Rightarrow N = \frac{A}{\lambda} = \frac{420}{4.919 \times 10^{-18}} = 8.537 \times 10^{19}$$

(1) Atomic Number Z	(2) Element	(3) Symbol	(4) Mass Number A	(5) Atomic Mass	(6) % Abundance (or Radioactive Decay Mode)	(7) Half-life (if radioactive)
86	Radon	Rn	222	222.017578	α, γ	3.8235 day
87	Francium	Fr	223	223.019736	β^-, γ, α	22.00 min
88	Radium	Ra	226	226.025410	α, γ	1600 yr
89	Actinium	Ac	227	227.027752	β^-, γ, α	21.772 yr
90	Thorium	Th	228	228.028741	α, γ	1.9116 yr
			232	232.038056	100%; α, γ	1.40×10^{10} yr
91	Protactinium	Pa	231	231.035884	α, γ	3.276×10^4 yr
92	Uranium	U	232	232.037156	α, γ	68.9 yr
			233	233.039636	α, γ	1.592×10^5 yr
			235	235.043930	0.7204%; α, γ	7.04×10^8 yr
			236	236.045568	α, γ	2.342×10^6 yr
			238	238.050788	99.2742%; α, γ	4.468×10^9 yr
			239	239.054294	β^-, γ	23.45 min
93	Neptunium	Np	237	237.048174	α, γ	2.144×10^6 yr
			239	239.052939	β^-, γ	2.356 days
94	Plutonium	Pu	239	239.052164	α, γ	24,110 yr
			244	244.064205	α	8.00×10^7 yr
95	Americium	Am	243	243.061381	α, γ	7370 yr
96	Curium	Cm	247	247.070354	α, γ	1.56×10^7 yr
97	Berkelium	Bk	247	247.070307	α, γ	1380 yr
98	Californium	Cf	251	251.079589	α, γ	898 yr
99	Einsteinium	Es	252	252.082980	$\alpha, \text{EC}, \gamma$	471.7 days
100	Fermium	Fm	257	257.095106	α, γ	100.5 days
101	Mendelevium	Md	258	258.098431	α, γ	51.5 days
102	Nobelium	No	259	259.101030	α, EC	58 min
103	Lawrencium	Lr	262	262.109610	$\alpha, \text{EC}, \text{fission}$	≈ 4 h
104	Rutherfordium	Rf	263	263.112500	fission	10 min
105	Dubnium	Db	268	268.125670	fission	32 h
106	Seaborgium	Sg	271	271.133930	$\alpha, \text{fission}$	2.4 min
107	Bohrium	Bh	274	274.143550	$\alpha, \text{fission}$	0.9 min
108	Hassium	Hs	270	270.134290	α	22 s
109	Meitnerium	Mt	278	278.156310	$\alpha, \text{fission}$	8 s
110	Darmstadtium	Ds	281	281.164510	$\alpha, \text{fission}$	20 s
111	Roentgenium	Rg	281	281.166360	$\alpha, \text{fission}$	26 s
112	Copernicium	Cn	285	285.177120	α	30 s
113 [†]			286	286.18210	$\alpha, \text{fission}$	20 s
114	Flerovium	Fl	289	289.190420	α	2.7 s
115 [†]			289	289.193630	$\alpha, \text{fission}$	0.22 s
116	Livermorium	Lv	293	293.204490	α	53 ms
117 [†]			294	294.210460	α	0.08 s
118 [†]			294	294.213920	$\alpha, \text{fission}$	0.9 ms

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$$\lambda = \frac{\ln 2}{t_{\frac{1}{2}}}$$

$$\lambda = \frac{\ln 2}{1.248 \times 10^9 \text{ yr}}$$

$$\lambda = 5.55 \times 10^{-10} \text{ yr}^{-1}$$

$$\lambda (\text{yr}^{-1}) \longrightarrow \lambda (\text{s}^{-1}):$$

$$\frac{5.55 \times 10^{-10}}{1 \text{ yr}} \times \frac{1 \text{ yr}}{365 \text{ days}} \times \frac{1 \text{ day}}{24 \text{ h}} \times \frac{1 \text{ h}}{60 \text{ min}} \times \frac{1 \text{ min}}{60 \text{ s}}$$

$$\lambda = 1.761182 \times 10^{-17} \text{ s}^{-1}$$

$$A_0 = \lambda N_0 \rightarrow N_0 = \frac{A_0}{\lambda} = \frac{2.4 \times 10^5 \frac{\text{decays}}{\text{s}}}{1.761182 \times 10^{-17} \frac{1}{\text{s}}} = 1.3627 \times 10^{22} \text{ particles.}$$

decay Rate → A_0
← decay Constant λ

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$$A = A_0 e^{-\lambda t}$$

$$t = 9.4 \text{ min} \rightarrow A = \frac{1}{6} A_0$$

$$\frac{1}{6} A_0 = A_0 e^{-\lambda(9.4)}$$

$$\frac{1}{6} = e^{-9.4\lambda}$$

$$\ln\left(\frac{1}{6}\right) = e^{-9.4\lambda}$$

$$\ln(6^{-1}) = \ln(e^{-9.4\lambda})$$

$$-\ln 6 = -9.4\lambda (\ln e)$$

$$\frac{\ln 6}{9.4} = \lambda$$

$$0.1906 \text{ min}^{-1} = \lambda$$

$$\lambda = \frac{\ln 2}{t_{\frac{1}{2}}} \Rightarrow t_{\frac{1}{2}} = \frac{\ln 2}{\lambda} = \frac{\ln 2}{0.1906} = 3.64 \text{ min}$$